

$$R_{\mathrm{H\,II}} = \left(\frac{3Q_{\mathrm{ion}}}{4\pi\alpha_{\mathrm{rec,B}}n_{\infty}^2} \right)^{1/3}$$