

$$\left(\frac{n_{\infty}}{10^5\text{ cm}^{-3}}\right)\left(\frac{M_{\text{BH}}}{10^4\text{ M}_{\odot}}\right)\gtrsim\left(\frac{T_{\infty}}{10^4\text{ K}}\right)^{3/2}$$