

$$R_{\text{HII}} = \left( \frac{3Q_{\text{ion}}}{4\pi\alpha_{\text{rec,B}}n_{\infty}^2} \right)^{1/3}$$